

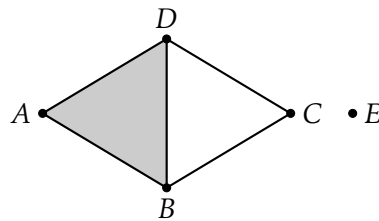
Computational topology

Lab work, 13th week

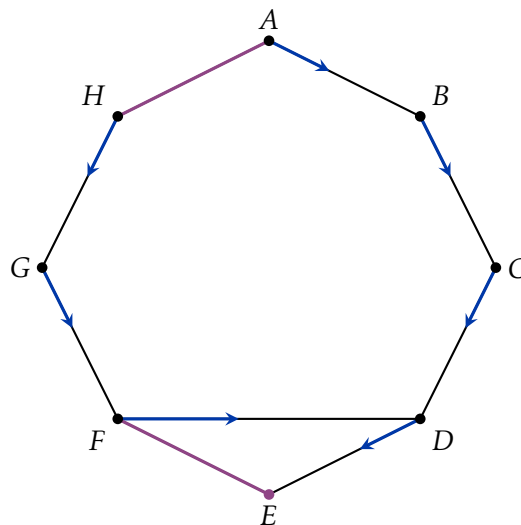
1. For a given simplicial complex K the function G is defined by the values in the following array.

σ	A	B	C	D	E	AB	AD	BC	BD	CD	ABD
$G(\sigma)$	3	2	0	3	2	6	4	1	4	1	5

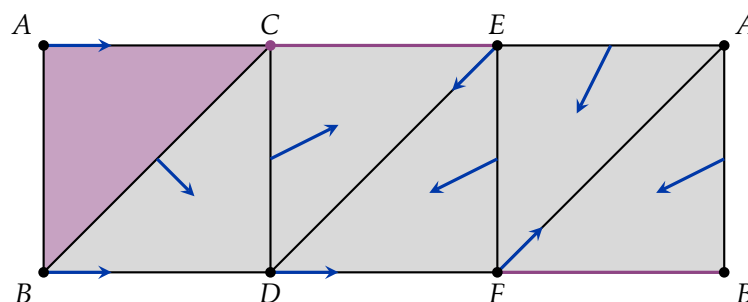
- Show that G is discrete Morse function on K .
- Determine the critical simplices and draw the corresponding vector field V_G .
- Find all non-trivial gradient paths and use cancellation to obtain a new vector field with the minimal possible number of critical simplices.



2. Use the given discrete vector field to compute the homology of this simplicial complex.



- Using the triangulations given in the following problems, construct an example of a discrete Morse function with a minimal number of critical simplices for the cylinder and the projective plane.
- Use the given discrete vector field on the cylinder to compute its homology.



5. Use the given discrete vector field on the projective plane \mathbb{RP}^2 to compute its homology.

