

# Mehanika

## Kinematika

$$s = \int_{r_0}^r |dr|$$

$$\mathbf{v} = \frac{dr}{dt}$$

$$\mathbf{a} = \frac{dv}{dt}$$

### Enakomerno pospešeno gibanje

$$v = v_0 + at$$

$$s = s_0 + v_0t + \frac{1}{2}at^2$$

$$v^2 = v_0^2 + 2as$$

### Poševni met

$$x = v_0t \cos \beta$$

$$z = v_0t \sin \beta - \frac{1}{2}gt^2$$

$$z = x \tan \beta - \frac{gx^2}{2v_0^2 \cos^2 \beta}$$

$$\boldsymbol{\omega} = \frac{d\varphi}{dt}, \quad \varphi = \frac{s}{r}$$

$$\boldsymbol{\alpha} = \frac{d\boldsymbol{\omega}}{dt}, \quad \mathbf{v} = \boldsymbol{\omega} \times \mathbf{r}$$

$$a_r = \omega^2 r = \frac{v^2}{r}$$

$$R_{kriv} = \frac{v^2}{a_r} = \frac{r^2}{\sqrt{a^2 - a_t^2}} = \frac{r^2}{\sqrt{\dot{r}^2 - a_t^2}}$$

## Dinamika

$$\mathbf{F} = m\mathbf{a}$$

$$\rho = \frac{dm}{dV}$$

$$\mathbf{F} = k\mathbf{s} \quad (\text{Hookov zakon})$$

$$\mathbf{M} = D\varphi$$

$$F_{tr} = k_{tr}F_{\perp}$$

$$F_{l,max} = k_l F_{\perp}$$

$$\mathbf{r}^* = \sum_i \frac{m_i \mathbf{r}_i}{m} = \int \frac{\mathbf{r} dm}{m} = \int \frac{\mathbf{r} dV}{V} = \iiint \frac{\mathbf{r} dx dy dz}{V}$$

$$\sum \mathbf{F}_{zun} = m\mathbf{a}^*$$

$$\mathbf{p} = \frac{d\mathbf{F}}{dS} \quad (\text{tlak})$$

$$\mathbf{f} = \frac{d\mathbf{F}}{dV} \quad (\text{gostota sile})$$

$$\mathbf{F}_s = -m\mathbf{a}_s \quad (\text{sistemska sila})$$

$$\mathbf{F}_{cf} = -m\boldsymbol{\omega} \times (\boldsymbol{\omega} \times \mathbf{r}) \quad (\text{centrifugalna sila})$$

$$\mathbf{F}_{Cor} = -2m\boldsymbol{\omega} \times \mathbf{v} \quad (\text{Coriolisova sila})$$

## Gibalna količina

$$\int \mathbf{F} dt = m\mathbf{v} - m\mathbf{v}_0 = \Delta \mathbf{G}$$

$$\mathbf{F} = \frac{d\mathbf{G}}{dt}$$

### Spošten trk v 1D ( $v_2' = 0$ )

$$v_1 = \frac{1-m_2/m_1}{1+m_2/m_1} v_1' \quad v_2 = \frac{2}{1+m_2/m_1} v_1'$$

$$\phi_m = \frac{dm}{dt} = \rho \phi_V$$

$$\phi_V = \frac{dV}{dt} = S \frac{dx}{dt} = Sv$$

$$\mathbf{F} = \phi_m (\mathbf{v}_0 - \mathbf{v}) \quad (\text{sila curka})$$

## Energija

$$A = \int \mathbf{F} \cdot d\mathbf{s} = \int (\mathbf{F} \cdot \mathbf{v}) dt$$

$$P = \frac{dA}{dt} = \mathbf{F} \cdot \mathbf{v}$$

$$\Delta W_k = \frac{1}{2}mv^2 - \frac{1}{2}mv_0^2 = \frac{1}{2} \frac{G^2}{m} - \frac{1}{2} \frac{G_0^2}{m}$$

$\oint \mathbf{F} \cdot d\mathbf{s} = 0 \implies$  konzervativna sila, lahko pripišemo potencialno energijo, delo sile je neodvisno od vmesne poti

$$A' = \Delta W_k - A_{konz} = \Delta W_k + \Delta W_p$$

$$\Delta W_{p,g} = mg\Delta h$$

$$\Delta W_{p,pr} = \frac{1}{2}k(x^2 - x_0^2) = \frac{1}{2}D(\varphi^2 - \varphi_0^2)$$

$A = \int \mathbf{F} \cdot d\mathbf{s} = \int \mathbf{F} \cdot d\mathbf{s}^* + \int \mathbf{F} \cdot d\mathbf{s}'$  (premik težišča in premik prijemališča sile glede na težišče)

## Vrtenje

$$\mathbf{M} = \mathbf{r} \times \mathbf{F}$$

$$J = \int dm r^2$$

$$J = J^* + md^2 \quad (\text{Steinerjev izrek})$$

$$\mathbf{M} = J\boldsymbol{\alpha}$$

### Vztrajnostni momenti nekaterih teles:

$$\text{Homogena palica okoli težišča: } J = \frac{1}{12}ml^2$$

$$\text{Valj okoli težišča vzdolž višine: } J = \frac{1}{2}m(r_1^2 + r_2^2)$$

$$\text{Votla krogla okoli težišča: } J = \frac{2}{3}mr^2$$

$$\text{Polna krogla okoli težišča: } J = \frac{2}{5}mr^2$$

$$A = \int Md\varphi$$

$$W_k = \frac{1}{2}mv^{*2} + \frac{1}{2}J^*\omega^2 \quad (\text{samo za togo telo in ne za sistem})$$

$$\boldsymbol{\Gamma} = J\boldsymbol{\omega} \quad (2D)$$

$$\boldsymbol{\Gamma} = \int d\boldsymbol{\Gamma} = \int \mathbf{r} \times d\mathbf{G} = \underline{J}\boldsymbol{\omega}$$

$$\underline{J} = \begin{bmatrix} \int dm (y^2 + z^2) & -\int dm xy & -\int dm xz \\ -\int dm yx & \int dm (x^2 + z^2) & -\int dm yz \\ -\int dm zx & -\int dm zy & \int dm (x^2 + y^2) \end{bmatrix}$$

$$\sum \mathbf{M}_{zun} = \frac{d\boldsymbol{\Gamma}}{dt}$$

$$\boldsymbol{\Gamma} = \boldsymbol{\Gamma}_0 + \boldsymbol{\Gamma}^* = m\mathbf{r}^* \times \mathbf{v}^* + \int \mathbf{r}' \times \mathbf{v}' dm$$

$$\mathbf{M}^* = \mathbf{r}' \times \mathbf{F} = \frac{d\boldsymbol{\Gamma}^*}{dt} \quad (\text{lastna vrtilna količina})$$

$$\mathbf{M}_0 = \mathbf{r}^* \times \mathbf{F} = \frac{d\boldsymbol{\Gamma}_0}{dt} \quad (\text{tirna vrtilna količina})$$

$$\mathbf{M}^* = \boldsymbol{\omega}_p \times \boldsymbol{\Gamma}^* \quad (\text{precesija})$$

## Deformacije

$$\frac{F_x}{S_x} = -E \frac{\Delta x}{x}$$

$$\frac{F_x}{S_y} = G \frac{\Delta x}{y}$$

$$\frac{F_x}{S} = -K \frac{\Delta V}{V}, \quad \chi^{-1} = K$$

$$\frac{\Delta y}{y} = \frac{\Delta z}{z} = -\mu \frac{\Delta x}{x}$$

$$K = \frac{E}{3(1-2\mu)}$$

$$G = \frac{E}{2(1+\mu)}$$

$$D = \frac{1}{2} \pi G \frac{r^4}{l}$$

Območje sorazmernosti (*meja linearnosti*),

območje prožnosti (*meja prožnosti*),

območje plastičnosti (*meja natezne trdnosti*).

## Gravitacija

$$\mathbf{F}_g = \kappa \frac{m_1 m_2}{(r_2 - r_1)^2} \frac{r_2 - r_1}{|r_2 - r_1|}$$

$$W_{p,g} = -\kappa \frac{m_1 m_2}{r}$$

### Keplerjevi zakoni

1. Planet se giblje po elipsi s Soncem v središču.

2. Ploščinska hitrost planeta je konstantna.

$$3. \frac{a^3}{T^2} = \frac{\kappa(M+m)}{4\pi^2}$$

Težnostni pospešek v okolici kroglastega telesa:

$$r > r_0 : g = g_0 \frac{r_0^2}{r^2}$$

$$r < r_0 : g = g_0 \frac{r}{r_0}$$

$$W = \frac{1}{2}mv^2 - \frac{\kappa Mm}{r} = \frac{1}{2}mv_0^2 - \frac{\kappa Mm}{r_0}$$

$W > 0 \implies$  telo se giblje po hiperboli.

$W = 0 \implies$  telo se giblje po paraboli.

$W < 0 \implies$  telo se giblje po elipsi.

## Hidrostatika

$$p = \frac{F}{S} = p_0 + \rho gh$$

$$\mathbf{F}_v = \int \mathbf{p} dS = -m_t \mathbf{g}$$

$$pV = p_0 V_0 \quad (\text{Boyllov zakon za pline})$$

$$\frac{dV}{V} = -\chi dp$$

$$F = \gamma b$$

$$W_{p,pov} = \gamma S$$

$$\Delta p = \frac{2\gamma}{R} \quad (\text{kapljica})$$

$$\Delta p = \frac{4\gamma}{R} \quad (\text{mehurček})$$

$$h = \frac{2\gamma \cos \theta}{\rho g r} \quad (\text{kapilarni dvig v valjasti kapilari})$$

## Hidrodinamika

$$dA = -p dV$$

$$\frac{F_s}{S_s} = \eta \frac{dv_x}{dz}$$

$$\Phi_V = \int \mathbf{v} \cdot d\mathbf{S}$$

$$v_s = \frac{\Phi_V}{S} = \frac{\int \mathbf{v} \cdot d\mathbf{S}}{\int dS} \quad (\text{srednja hitrost})$$

$$\Phi_m = \Phi_{m0} \quad (\text{kontinuitetna enačba})$$

$$p_0 + \frac{1}{2}\rho v_0^2 + \rho g z_0 \geq p + \frac{1}{2}\rho v^2 + \rho g z$$

$$p = p_0 + \frac{1}{2}\rho v_0^2 \quad (\text{zastojni tlak})$$

$$F_u = \frac{1}{2}c_u \rho v^2 S \quad (Re > 10^3)$$

$$F_u = c_l \eta v \quad (Re < 0,5)$$

$$F_u = 6\pi R \eta v = \frac{24}{Re} \frac{1}{2} \rho v^2 S \quad (\text{Stokesov zakon za kroglo})$$

$$Re = \frac{\rho v r}{\eta} = \frac{2R\rho v}{\eta}$$

$$v = v_0 \left(1 - \frac{r^2}{R^2}\right), \quad v_0 = \frac{R^2(p_0 - p)}{4l\eta} \quad (\text{valjasta cev, } Re < 2300)$$

$$\Phi_V = v_s \pi R^2 = \frac{\pi R^4 (p_0 - p)}{8l\eta} \quad (\text{Poiseuillov zakon})$$

## Nihanje

$$\omega_0 = \sqrt{k/m}$$

$$\omega_0 = \sqrt{g/l}$$

$$\omega_0 = \sqrt{D/J}$$

$$\omega_0 = \sqrt{mgd/J}$$

$$s = s_0 \cos(\omega t + \delta) = s_1 \cos \omega t + s_2 \sin \omega t$$

$$s_1 = s_0 \cos \delta, \quad s_2 = -s_0 \sin \delta$$

$$s = s_0 \cos \omega_1 t + s_0 \cos \omega_2 t =$$

$$= 2s_0 \cos\left(\frac{1}{2}(\omega_2 - \omega_1)t\right) \cos\left(\frac{1}{2}(\omega_2 + \omega_1)t\right) = 2s_0 \cos \frac{1}{2}\omega_u t \cos \omega t$$

## Dušeno nihanje

$$W = W_0 e^{-2\beta t}, \quad F_u = -2\beta m v$$

$$\omega^2 = \omega_0^2 - \beta^2$$

**Podkritično dušenje** ( $\omega_0 > \beta$ )

$$s = s_0 e^{-\beta t} \cos(\omega t + \delta)$$

$$A = -\ln \frac{s(t+T)}{s(t)} = \beta T = \frac{2\pi\beta}{\omega}$$

**Kritično dušenje** ( $\omega_0 = \beta$ )

$$s = s_1 e^{-\beta t} + s_2 t e^{-\beta t}$$

**Nadkritično dušenje** ( $\omega_0 < \beta$ )

$$s = s_0 e^{-\beta t} \cosh(\omega t + \delta)$$

## Vsiljeno nihanje

$$\ddot{x} + 2\beta\dot{x} + \omega_0^2 x = \omega_0^2 s_0 \cos \omega t$$

$$x = x_1 e^{-\beta t} \cos\left(\sqrt{\omega_0^2 - \beta^2}t - \delta'\right) + x_0 \cos(\omega t - \delta)$$

$$w = \omega/\omega_0$$

$$\tan \delta = \frac{2\beta}{\omega_0} \frac{w}{1-w^2}$$

$$\frac{x_0}{s_0} = \left((1-w^2)^2 + \left(\frac{2\beta}{\omega_0}\right)^2 w^2\right)^{-\frac{1}{2}}$$

$$\bar{P} = \mathbf{F} \cdot \mathbf{v} = \beta m \omega_0^2 s_0^2 \frac{w^2}{(1-w^2)^2 + \left(\frac{2\beta}{\omega_0}\right)^2 w^2}$$

$$\omega_{1/2} = 2\beta, \quad \bar{P}(\omega_0 + \frac{1}{2}\omega_{1/2}) = \bar{P}(\omega_0 - \frac{1}{2}\omega_{1/2}) = \frac{1}{2}\bar{P}_{max}$$

## Valovanje

$$c = \sqrt{\frac{F}{\rho S}} \quad (\text{transverzalna motnja na napeti vrvici})$$

$$c = \sqrt{\frac{E}{\rho}} = \sqrt{\frac{k}{m} l} \quad (\text{longitudinalna motnja v trdnini})$$

$$c = \frac{1}{\sqrt{\chi\rho}} = \sqrt{\frac{\kappa p}{\rho}} \quad (\text{longitudinalna motnja v kapljevini in plinu})$$

$$w = \frac{dW}{dV} = \rho v^2 \quad w_k = w_p = \frac{1}{2}\rho v^2 \quad (\text{transverzalna motnja})$$

**Splošno**

$$w_k = \frac{1}{2}\rho v^2 = \frac{1}{2}\rho \left(\frac{\partial s}{\partial t}\right)^2$$

$$w_p = \frac{1}{2}c^2 \rho \left(\frac{\partial s}{\partial x}\right)^2$$

$$\delta p = -c^2 \rho \frac{\partial s}{\partial x}$$

## Valovanje v eni razsežnosti

$$s = s_0 \cos(kx - \omega t)$$

$$k = \frac{2\pi}{\lambda} = \frac{\omega}{c} \quad \omega = 2\pi\nu \quad c = \nu\lambda$$

$$w = \rho v^2 = \rho \omega^2 s_0^2 \sin^2(\omega t - kx)$$

$$\bar{w} = \frac{1}{2}\rho \omega^2 s_0^2$$

$$j = \frac{P}{S} = \frac{\bar{W}}{S t} = c\bar{w} = \frac{1}{2}c\rho\omega^2 s_0^2 = \frac{1}{2} \left(\frac{\delta p}{\rho c}\right)_0^2$$

**Interferenca**

$$s = s_1 + s_2 = s_0 \cos(\omega t - kx) + s_0 \cos(\omega t - kx + \delta) =$$

$$= 2s_0 \cos \frac{1}{2}\delta \cos\left(\omega t - kx + \frac{1}{2}\delta\right) = S_0 \cos(\omega t - kx + \Delta)$$

Na prostem krajišču se valovanje odbije z enako fazo, na vpetem krajišču pa z nasprotno fazo.

**Stoječe valovanje**

$$s = s_1 \cos(\omega t - kx) + s_1 \cos(\omega t + kx) = 2s_1 \cos kx \cos \omega t$$

$$\nu_N = \frac{1}{2}(N+1)\frac{c}{l} \quad (\text{dve vpeti ali dve prosti krajišči})$$

$$\nu_N = \frac{1}{4}(2N+1)\frac{c}{l} \quad (\text{eno vpeto in eno prosto krajišče})$$

$$w = \frac{1}{2}\rho\omega^2 s_0^2 (\sin^2 kx \sin^2 \omega t + \cos^2 kx \cos^2 \omega t)$$

$$\bar{w} = \frac{1}{4}\rho\omega^2 s_0^2$$

**Valovanje več razsežnostih**

$$\mathbf{k} = \frac{2\pi}{\lambda} \frac{c}{c}$$

$$\mathbf{s} = \mathbf{s}_0(\mathbf{r}) \cos(\mathbf{k} \cdot \mathbf{r} - \omega t) \quad (\text{ravni val})$$

$$\mathbf{s} = \mathbf{s}_0(r) \cos(kr - \omega t) \quad (\text{krogelni val})$$

**Interferenca**

$$\text{maksimumi: } a \sin \beta = n\lambda \quad (\text{daleč od izvira})$$

$$\text{minimumi: } a \sin \beta = (2n+1)\frac{1}{2}\lambda \quad (\text{daleč od izvira})$$

**Dopplerjev pojav**

$$\nu' = \nu \frac{1+v_s/c}{1-v_i/c}$$

$$\lambda' = \lambda \frac{1-v_i/c}{1+v_s/c}$$

**Disperzija** je pojav, pri katerem je hitrost valovanja odvisna od valovne dolžine.

$$c = \sqrt{\frac{g}{k} + \frac{\gamma k}{\rho}} \quad (\text{valovanje na vodni gladini v globoki vodi})$$

$$c = \sqrt{gh} \quad (\text{valovanje na vodni gladini v plitvi vodi})$$

$$c_g = \left(\frac{dc}{dk}\right)_{\omega_0} = c_f + k \left(\frac{dc}{dk}\right)_{\omega_0} = c_f - \lambda \left(\frac{dc}{d\lambda}\right)_{\lambda_0}$$

**Zvok**

$$\text{glasnost} = 10 \log \frac{j}{j_0(\nu)} [\text{fon}]$$

$$\text{jakost neodvisna od frekvence: } 10 \log \frac{j}{j_0} [\text{dB}]$$

## Termodinamika

**0. zakon termodinamike:** Če sta v ravnovesju 1. in 2.

sistem, ko sta med seboj v toplotnem stiku, a sta adiabatsno izolirana od okolice, in če sta v ravnovesju 2. in 3. sistem, ko sta med seboj v toplotnem stiku, a sta adiabatsno izolirana od okolice, sta v ravnovesju tudi 1. in 3. sistem.

**Temperaturno raztezanje**

$$dl = \alpha l dT$$

$$dV = \beta V dT$$

$$\beta = 3\alpha$$

$$\frac{dV}{V} = -\chi_T dp + \beta_p dT$$

**Energijski zakon**

**1. zakon termodinamike:**

$$W_n \text{ je funkcija stanja in } dW_n = dQ + dA$$

$$dA = -p dV \quad (\text{če so vsa vmesna stanja definirana})$$

$$H = W_n + pV \quad (\text{entalpija - funkcija stanja})$$

$$dH = dQ + V dp$$

$$(dW_n)_V = (dQ)_V = mc_V dT$$

$$(dH)_p = (dQ)_p = mc_p dT$$

$$\Delta H = (Q)_p = qm \quad (\text{poljuben fazni prehod})$$

$$P = \frac{dQ}{dt}$$

$$\mathbf{j} = -\lambda \nabla T \quad (\text{prevajanje v 3 dimenzijah})$$

$$j = -\lambda \frac{dT}{dx} \quad (\text{prevajanje v 1 dimenziji})$$

$$P = -\Lambda \dot{S}(T - T_0) \quad (\text{konvekcija})$$

## Entropijski zakon

**2. zakon termodinamike:**  $S$  je funkcija stanja in

$$\Delta S \geq \int \frac{dQ}{T} \quad (\text{enakost pri reverzibilnih spremembah})$$

$$S = k_B \ln w \quad (w \text{ je število mikroskopskih stanj})$$

**Clausius-Clapeyronova enačba**

$$\frac{dp_s}{p_s} = \frac{M q_i(T)}{R} \frac{dT}{T^2}$$

$$p_s = p_{s0} e^{\frac{M q_i}{R} \left(\frac{1}{T_0} - \frac{1}{T}\right)} \quad (\text{približek } q_i = \text{konst.})$$

$$\frac{dp}{dT} = \frac{q_t}{T \left(\frac{1}{\rho_{\text{kaplj}}} - \frac{1}{\rho_{\text{trd}}}\right)}$$

## Toplotni stroji

$$Q_{\text{dov}} = |A| + |Q_{\text{odv}}|$$

$$\eta = \frac{|A|}{Q_{\text{dov}}} = 1 - \frac{|Q_{\text{odv}}|}{Q_{\text{dov}}}$$

$$\eta_C = 1 - \frac{T_{\text{min}}}{T_{\text{max}}} \quad (\text{Carnotov stroj})$$

$$\eta_C = \frac{Q_{\text{dov}}}{A} = \frac{T}{T_0 - T} \quad (\text{Carnotov hladilnik})$$

$$\eta_C = \frac{Q_{\text{odv}}}{A} = \frac{T_0}{T_0 - T} \quad (\text{Carnotova toplotna črpalka})$$

## Idealni plin

$$pV = \frac{m}{M} RT$$

$$\rho = \frac{pM}{RT}$$

$$\beta_p = \frac{1}{T}$$

$$\chi_T = \frac{1}{p}$$

$$p = \sum p_{\text{parc}} \quad (\text{Daltonov zakon})$$

$$W_n = mc_V T \quad (\text{vedno})$$

$$H = mc_p T \quad (\text{vedno})$$

$$\Delta S = mc_V \ln \frac{T}{T_0} + m \frac{R}{M} \ln \frac{V}{V_0} \quad (\text{vedno})$$

$$\kappa = \frac{c_p}{c_V}$$

$$c_p - c_V = \frac{R}{M}$$

$$c_p = \frac{\kappa}{\kappa-1} \frac{R}{M}, \quad c_V = \frac{1}{\kappa-1} \frac{R}{M}$$

**Spremembe**

|            | $\Delta W_n$    | $A$                          | $Q$                              |
|------------|-----------------|------------------------------|----------------------------------|
| izohorna   | $mc_V \Delta T$ | 0                            | $mc_V \Delta T$                  |
| izobarna   | $mc_V \Delta T$ | $-p \Delta V$                | $\Delta H = mc_p \Delta T$       |
| izoterma   | 0               | $-p_0 V_0 \ln \frac{V}{V_0}$ | $-A = p_0 V_0 \ln \frac{V}{V_0}$ |
| izentropna | $mc_V \Delta T$ | $mc_V \Delta T$              | 0                                |

Pri izentropni (adiabatni) spremembi še dodatno:

$$pV^\kappa = \text{konst.}$$

$$\chi_S = \frac{1}{\kappa p}$$

## Kinetična teorija plinov

$$n = \frac{dN}{dV}$$
$$p = \frac{2}{N_p} n \langle W_k \rangle = \frac{1}{N_p} n m_1 \langle v^2 \rangle$$
$$W_n = N \langle W_k \rangle = \frac{N_p}{2} N k_B T$$
$$\langle l \rangle = \frac{1}{\sqrt{2\pi} d^2 n} \quad (\text{povprečna prosta pot})$$
$$j_N = \frac{d^2 N}{dt dS} = \frac{1}{4} n \langle v \rangle$$
$$j_D = D \frac{dn}{dx}, \quad D = \frac{1}{3} \langle v \rangle \langle l \rangle \quad (\text{difuzija})$$
$$\frac{1}{N} \frac{d^3 N}{dv_x dv_y dv_z} = \left( \frac{m_1}{2\pi k_B T} \right)^{\frac{3}{2}} e^{-\frac{W_k}{k_B T}}$$
$$\frac{dN}{N dv} = 4\pi v^2 \left( \frac{m_1}{2\pi k_B T} \right)^{\frac{3}{2}} e^{-\frac{mv^2}{2k_B T}}$$

## Elektrika

### Električno polje

Naboj izoliranega sistema je konstanten.

Coulombov zakon:  $\mathbf{F} = -\frac{e_1 e_2}{4\pi\epsilon_0 (r_1 - r_2)^2} \frac{r_1 - r_2}{|r_1 - r_2|}$

$$\sigma = \frac{de}{dS}$$
$$\rho_e = \frac{de}{dV}$$

$$\mathbf{F} = e\mathbf{E}$$
$$\mathbf{D} = \epsilon\epsilon_0 \mathbf{E}$$
$$\phi_e = \int \mathbf{D} \cdot d\mathbf{S}$$

Gaussov zakon:  $\oint \mathbf{D} \cdot d\mathbf{S} = e$

$$dV = -\mathbf{E} \cdot d\mathbf{s}$$
$$\mathbf{E} = -\nabla V$$
$$U(\mathbf{r}, \mathbf{r}_1) = V(\mathbf{r}) - V(\mathbf{r}_1)$$
$$dA = U de$$
$$\oint \mathbf{E} \cdot d\mathbf{s} = 0$$
$$W_{p,e} = eV$$
$$w_e = \frac{dW_e}{dV} = \frac{1}{2} \epsilon\epsilon_0 E^2 = \frac{1}{2} ED$$

### Električni dipol

$$\mathbf{p}_e = e\mathbf{a}$$
$$W_p = -\mathbf{p}_e \cdot \mathbf{E}$$
$$\mathbf{M} = \mathbf{p}_e \times \mathbf{E}$$

Dipol v izhodišču na premici z:

$$E_x = \frac{3p_e \sin \vartheta \cos \vartheta}{4\pi\epsilon_0 r^3}, \quad E_y = 0, \quad E_z = \frac{p_e (3 \cos^2 \vartheta - 1)}{4\pi\epsilon_0 r^3}$$

### Snov v električnem polju

V prevodniku v stacionarnem stanju ni električnega polja.

$$P = np_{e,1} = \frac{dN}{dV} p_{e,1} \quad (\text{polarizacija})$$
$$e_p = PS \quad (\text{vezan naboj})$$
$$P = (\epsilon - 1)\epsilon_0 E = \chi\epsilon_0 E$$

### Električni tok

$$I = \frac{de}{dt}$$
$$j_e = \frac{dI}{dS}$$
$$\mathbf{j}_e = \rho_e \mathbf{v}$$
$$\mathbf{j}_e = \frac{d\mathbf{D}}{dt} \quad (\text{premikalni tok})$$

Prvi Kirchoffov izrek:  $\sum I_{\text{pri}} = \sum I_{\text{od}}$  v razvejišču

Drugi Kirchoffov izrek:  $\sum U_{\text{gon}} = \sum U_{\text{por}}$  v zanki

Ohmov zakon:  $U = RI$

$$R = \zeta \frac{l}{S}$$
$$d\zeta = \alpha \zeta dT$$
$$\mathbf{E} = \zeta \mathbf{j}_e$$

Zaporedno vezani uporniki:  $R = \sum_i R_i$

Vzporedno vezani uporniki:  $\frac{1}{R} = \sum_i \frac{1}{R_i}$

$$P = UI = I^2 R = \frac{U^2}{R}$$
$$\frac{dP}{dV} = \zeta j_e^2$$

### Izmenični tok

$$I = I_0 \cos \omega t = \text{Re}(I_0 e^{i\omega t}) \quad I_{ef} = \frac{1}{\sqrt{2}} I_0$$
$$U = U_0 \cos(\omega t + \delta) = \text{Re}(U_0 e^{i\omega t}) \quad U_{ef} = \frac{1}{\sqrt{2}} U_0$$
$$\bar{P} = \frac{1}{2} U_0 I_0 \cos \delta = U_{ef} I_{ef} \cos \delta$$

Ohmov zakon za kompleksno impedanco:  $U = ZI$

Zaporedno vezane komponente:  $Z = \sum_i Z_i$

Vzporedno vezane komponente:  $\frac{1}{Z} = \sum_i \frac{1}{Z_i}$

$$Z_R = R$$
$$Z_C = \frac{1}{i\omega C} \quad (\text{kapacitanca})$$
$$Z_L = i\omega L \quad (\text{induktanca})$$

### Transformator

$$U_1 = -L_{11} \frac{dI_1}{dt} - L_{12} \frac{dI_2}{dt}$$
$$U_2 = -L_{22} \frac{dI_2}{dt} - L_{21} \frac{dI_1}{dt}$$

Obremenjen z uporom:  $\frac{U_{ef,1}}{U_{ef,2}} = \frac{N_1}{N_2} = \frac{I_{ef,2}}{I_{ef,1}}$

### Kondenzatorji

$$e = CU$$
$$W_c = \frac{1}{2} CU^2 = \frac{1}{2} \frac{e^2}{C}$$

Ploščati kondenzator:  $C = \epsilon\epsilon_0 \frac{S}{l}$

Valjasti kondenzator:  $C = 2\pi\epsilon\epsilon_0 \frac{l}{\ln(r_1/r_2)}$

Krogelni kondenzator:  $C = 4\pi\epsilon\epsilon_0 \frac{r_1 r_2}{r_1 - r_2}$

Zaporedno vezani kondenzatorji:  $\frac{1}{C} = \sum_i \frac{1}{C_i}$

Vzporedno vezani kondenzatorji:  $C = \sum_i C_i$

Polnjenje kondenzatorja:  $U_c = U_0(1 - e^{-t/(RC)})$

Praznjenje kondenzatorja:  $U_c = U_0 e^{-t/(RC)}$

## Magnetizem

### Magnetno polje

$$\mathbf{F} = I\mathbf{l} \times \mathbf{B} = e\mathbf{v} \times \mathbf{B}$$
$$\mathbf{f} = \frac{d\mathbf{F}}{dV} = \mathbf{j}_e \times \mathbf{B}$$

$$\phi_m = \int \mathbf{B} \cdot d\mathbf{S}$$
$$\oint \mathbf{B} \cdot d\mathbf{S} = 0 \quad (\text{ni magnetnih monopolov})$$

$\mathbf{B} = \mu\mu_0 \mathbf{H}$

Amperov zakon:  $\oint \mathbf{H} \cdot d\mathbf{s} = I + \frac{\partial}{\partial t} \int \mathbf{D} \cdot d\mathbf{S} = I + \frac{d\phi_e}{dt}$

Biot-Savartov zakon:  $d\mathbf{H} = \frac{I}{4\pi} \frac{d\mathbf{l} \times \mathbf{r}}{r^3} = \frac{d\mathbf{e}}{4\pi} \frac{\mathbf{v} \times \mathbf{r}}{r^3}$  ( $\mathbf{r}$  ima smer od vodnik do neke točke)

$$w_e = \frac{1}{2} \mu\mu_0 H^2 = \frac{1}{2} \mathbf{H} \cdot \mathbf{B}$$

### Magnetni dipol

$$\mathbf{p}_m = IS$$
$$\mathbf{M} = \mathbf{p}_m \times \mathbf{B}$$
$$W_p = -\mathbf{p}_m \cdot \mathbf{B}$$

### Snov v magnetnem polju

Paramagnetna snov:  $\mu > 1$  (malo)

Diamagnetna snov:  $\mu < 1$  (malo)

Feromagnetna snov:  $\mu(H) = \frac{dB}{\mu_0 dH} \gg 1$

Diagram  $B(H)$  za feromagnetne snovi je *histerezna krivulja*.

$$M = n \langle p_{m,1} \rangle = \frac{dN}{dV} \langle p_{m,1} \rangle$$

$$I_M = MI$$

$$M = (\mu - 1) \frac{B_0}{\mu_0} = \chi \frac{B_0}{\mu_0}$$

### Indukcija

Faradayev zakon:  $\oint \mathbf{E} \cdot d\mathbf{s} = -\frac{\partial}{\partial t} \int \mathbf{B} \cdot d\mathbf{S}$

$$U_i = \frac{d\phi_m}{dt}$$

$$U_i = \mathbf{v} \cdot (\mathbf{B} \times \mathbf{l})$$

Gaussov zakon, zakon o magnetnem pretoku, Amperov zakon in Faradayev zakon so osnovni zakoni elektrodinamike ali Maxwelllove enačbe.

### Tuljava

$$\phi_m = LI$$

$$U_i = -L \frac{dI}{dt}$$

$$W_m = \frac{1}{2} LI^2 = \frac{1}{2} \frac{\phi_m^2}{L}$$

Dolga tuljava:  $L = \frac{\mu_0 N^2 S}{l}$

Tanek toroid:  $L = \frac{\mu_0 N^2 S}{2\pi r}$

Koaksialni vodnik:  $L = \frac{\mu_0 l}{2\pi} \ln\left(\frac{r_1}{r_2}\right)$

Polnjenje tuljave:  $I = I_0(1 - e^{-tR/L})$

Praznjenje tuljave:  $I = I_0 e^{-tR/L}$

Vzajemna induktivnost:  $L_{ij} = \frac{\mu_0 N_i N_j S}{l}$

### Nihajni krog

$$\omega_0 = (LC)^{-\frac{1}{2}}$$

$$W = W_m + W_e = \frac{1}{2} LI_0^2 = \frac{1}{2} CU_0^2$$

### Dušeno nihanje

$$\beta = \frac{R}{2L}$$

$$\omega_1 = \sqrt{\omega_0^2 - \beta^2}$$

$$I = I_0 e^{-\beta t} \cos \omega_1 t$$

### Vsiljeno nihanje

$$w = \omega/\omega_0$$

$$\tan \delta = \frac{1 - \omega^2 LC}{\omega RC}$$

$$\frac{I_0}{U_0/\omega_0 L} = w/\sqrt{(1 - w^2)^2 + \left(\frac{2\beta w}{\omega_0}\right)^2}$$

## Elektromagnetno valovanje

$$c_0 = \sqrt{1/\varepsilon_0\mu_0}$$

$$\mathbf{E} = \mathbf{B} \times \mathbf{c}$$

$$w = w_e + w_m = 2w_{m0} = 2w_{e0} = \varepsilon_0 E^2 = \frac{B^2}{\mu_0}$$

$$j = wc = \varepsilon_0 c E^2$$

$$\mathbf{j} = \mathbf{E} \times \mathbf{H} \quad (\text{Poyntingov vektor})$$

$$\bar{j} = \frac{1}{2} \varepsilon_0 c E_0^2 = \frac{1}{2} E_0 H_0$$

Vpadanje valovanja na prevodno ploščo:  $p = \bar{w}$

Točkasti izvor:

$$E(r, t) = E_0(r) \sin(kr - \omega t)$$

$$E_0 \propto \frac{1}{r} \quad B_0 \propto \frac{1}{r}$$

Polarizator:  $j = j_0 \cos^2 \vartheta$

## Elektromagnetno valovanje v koaksialnem vodniku

$$c = \sqrt{1/\varepsilon\varepsilon_0\mu_0} = c_0 \sqrt{1/\varepsilon}$$

$$Z_0 = \frac{U}{I} = \frac{\ln(b/a)}{2\pi} \sqrt{\frac{\mu_0}{\varepsilon\varepsilon_0}}$$

$$\frac{\partial I}{\partial x} = -C_l \frac{\partial U}{\partial t} - \left(\frac{1}{R}\right) I$$

$$\frac{\partial U}{\partial x} = -L_l \frac{\partial I}{\partial t} - R_l I$$

$$U_{\text{odb}} = -U_{\text{vpd}} \frac{Z_0 - Z}{Z_0 + Z}$$

$x = 0$ :  $U = U_0 e^{-i\omega t}$ , torej ima  $Z$  nasproten predznak kot ponavadi

## Valovna optika

$$n = \frac{c}{c_0}$$

$$R = \frac{j_v}{j_v} = \left(\frac{n_1 - n_2}{n_1 + n_2}\right)^2$$

$$T = \frac{j_p}{j_p} = \frac{4n_1 n_2}{(n_1 + n_2)^2}$$

Huyghensovo načelo: vsaka točka na valovni fronti je izvir točkastega valovanja.

## Tanka plast in kristalne ravnine

$$2nd \cos \beta = N\lambda \quad (\text{maksimumi})$$

$$2nd \cos \beta = (N + \frac{1}{2})\lambda \quad (\text{minimumi})$$

Če je število obratov faze liho, se pogoja zamenjata.

## Uklonska mrežica

$$j = j_0 \frac{\sin^2(N \frac{ka}{2} \sin \alpha)}{\sin^2(\frac{ka}{2} \sin \alpha)} = j_0 \frac{\sin^2 N \delta_n}{\sin^2 \delta_n}$$

$$a \sin \alpha = m\lambda \quad (\text{maksimumi})$$

## Široka reža

$$j = j_0 \frac{\sin^2(\frac{kb}{2} \sin \alpha)}{(\frac{kb}{2} \sin \alpha)^2} = j_0 \frac{\sin^2 \delta}{\delta^2}$$

$$b \sin \alpha = m\lambda \quad (\text{minimumi})$$

$$N \text{ rež: } j = j_0 \frac{\sin^2 N \delta_n}{\sin^2 \delta_n} \frac{\sin^2 \delta}{\delta^2}$$

## Fotometrija

$$\text{Prostorski kot: } d\Omega = \frac{dS}{r^2}$$

$$\text{Svetilnost: } I = \frac{dP}{d\Omega}$$

$$\text{Svetlost: } B_0 = \frac{I_0}{S}$$

## Absorpcija

$$j = j_0 e^{-\mu z}$$

$$l_{1/2} = \frac{\ln 2}{\mu}$$

## Toplotno sevanje

$$j_{\text{odp}} = aj_v \quad j_{\text{abs}} = (1 - a)j_v$$

$$j^* = (1 - a)\sigma T^4$$

$$\lambda_{\text{max}} T = k_W$$

## Geometrijska optika

Odbojni zakon: odbojni kot je enak vpadnemu

Lomni zakon:  $n_1 \sin \alpha = n_2 \sin \beta$

Če  $n_2 > n_1$ , se ob odboju faza spremeni za  $\pi$ .

$$\tan \alpha_{\text{Brew}} = \frac{n_2}{n_1}$$

$$\sin \alpha_{\text{tot}} = \frac{n_2}{n_1}$$

$$\text{Planparalelna plast: } d = h \frac{\sin(\alpha - \beta)}{\cos \beta}$$

## Zrcala

$$f = \frac{1}{2}r \quad (\text{negativna pri konveksnem zrcalu})$$

$$\frac{1}{f} = \frac{1}{a} + \frac{1}{b}$$

$$\frac{y'}{y} = \frac{b}{a} \quad (\text{povečava})$$

$$\tan \alpha = \frac{y}{a} \quad (\text{zorni kot oddaljenega telesa})$$

## Tanke leče

$$\frac{1}{f} = (n - 1) \left( \frac{1}{r} + \frac{1}{r'} \right) \quad (\text{negativna pri konkavi leči})$$

$$\frac{1}{f} = \frac{1}{a} + \frac{1}{b}$$

$$\frac{y'}{y} = \frac{b}{a} \quad (\text{povečava})$$

## Fizikalne konstante

$$g = 9,81 \frac{\text{m}}{\text{s}^2}$$

$$\kappa = 6,67408 \cdot 10^{-11} \frac{\text{m}^3}{\text{kg s}^2}$$

$$r_Z = 6400 \text{ km} \quad (\text{polmer Zemlje})$$

$$m_Z = 6 \cdot 10^{24} \text{ kg} \quad (\text{masa Zemlje})$$

$$m_S = 2 \cdot 10^{30} \text{ kg} \quad (\text{masa Sonca})$$

$$d_{ZS} = 1,5 \cdot 10^8 \text{ km} \quad (\text{razdalja Zemlja - Sonce})$$

$$d_{ZL} = 384 000 \text{ km}$$

$$j_0 = 10^{-12} \frac{\text{W}}{\text{m}^2}$$

$$p_0 = 10^5 \text{ Pa} \quad (\text{tlak na gladini morja})$$

$$c_{H_2O} = 4 200 \frac{\text{J}}{\text{kg K}} \quad (\text{specifična toplota vode})$$

$$q_t = 334 \frac{\text{kJ}}{\text{kg}} \quad (\text{specifična talilna entalpija vode})$$

$$q_i = 2 264 \frac{\text{kJ}}{\text{kg}} \quad (\text{specifična izparilna entalpija vode})$$

$$R = 8 310 \frac{\text{J}}{\text{kmol K}}$$

$$N_A = 6,02 \cdot 10^{26} \frac{1}{\text{kmol}}$$

$$k_B = \frac{R}{N_A} = 1,38 \cdot 10^{-23} \frac{\text{J}}{\text{K}}$$

$$M_{\text{zrak}} = 29 \frac{\text{kg}}{\text{kmol}}$$

$$N_{p1} = 3, \quad N_{p2} = 5 \quad (\text{prostorske stopnje})$$

$$\kappa_1 = \frac{5}{3}, \quad \kappa_2 = \frac{7}{5}$$

$$e_0 = 1,602 \cdot 10^{-19} \text{ As}$$

$$\varepsilon_0 = 8,85 \cdot 10^{-12} \frac{\text{As}}{\text{Vm}}$$

$$\mu_0 = 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}}$$

$$c_0 = 3,0 \cdot 10^8 \frac{\text{m}}{\text{s}}$$

$$\sigma = 5,67 \cdot 10^{-8} \frac{\text{W}}{\text{m}^2 \text{K}^4}$$

$$k_W = 2,90 \cdot 10^{-3} \text{ m} \cdot \text{K}$$

$$u = 1,66 \cdot 10^{-27} \text{ kg} = 931,5 \frac{\text{MeV}}{c^2}$$

$$m_e = 9,1 \cdot 10^{-31} \text{ kg} = 0,511 \frac{\text{MeV}}{c^2}$$

$$m_p = 1,673 \cdot 10^{-27} \text{ kg} = 938,3 \frac{\text{MeV}}{c^2} = 1,00728u$$

$$m_n = 1,675 \cdot 10^{-27} \text{ kg} = 939,6 \frac{\text{MeV}}{c^2} = 1,00866u$$

## Trigonometrične identitete

$$\sin^2 \alpha + \cos^2 \alpha = 1$$

$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$$

$$\tan(\alpha \pm \beta) = \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta}$$

$$\sin 2\alpha = 2 \sin \alpha \cos \alpha$$

$$\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha = 2 \cos^2 \alpha - 1 = 1 - 2 \sin^2 \alpha$$

$$\sin \alpha + \sin \beta = 2 \sin \frac{\alpha + \beta}{2} \cos \frac{\alpha - \beta}{2}$$

$$\sin \alpha - \sin \beta = 2 \cos \frac{\alpha + \beta}{2} \sin \frac{\alpha - \beta}{2}$$

$$\cos \alpha + \cos \beta = 2 \cos \frac{\alpha + \beta}{2} \cos \frac{\alpha - \beta}{2}$$

$$\cos \alpha - \cos \beta = -2 \sin \frac{\alpha + \beta}{2} \sin \frac{\alpha - \beta}{2}$$

$$\tan \alpha \pm \tan \beta = \frac{\sin(\alpha \pm \beta)}{\cos \alpha \cos \beta}$$

## Diferencialne enačbe

$$\ddot{x} = -\omega^2 x \implies \frac{1}{2} m \dot{x}^2 + \frac{1}{2} m \omega^2 x^2 = W \implies$$

$$x = A \sin(\omega t) + \tilde{B} \cos(\omega t)$$

$$\ddot{x} = \omega^2 x \implies x = A \sinh(\omega t) + B \cosh(\omega t)$$

$$\frac{1}{c^2} \frac{\partial^2 s}{\partial t^2} = \frac{\partial^2 s}{\partial x^2} \implies s = A \cos(kx - \omega t + \delta)$$

## Koordinatni sistemi

$$\mathbf{r} = x\hat{\mathbf{e}}_x + y\hat{\mathbf{e}}_y + z\hat{\mathbf{e}}_z \quad (\text{kartezični koordinatni sistem})$$

$$\mathbf{r} = \rho\hat{\mathbf{e}}_\rho + \varphi\hat{\mathbf{e}}_\varphi + z\hat{\mathbf{e}}_z \quad (\text{cilindrični koordinatni})$$

$$\mathbf{r} = r\hat{\mathbf{e}}_r + \varphi\hat{\mathbf{e}}_\varphi + \vartheta\hat{\mathbf{e}}_\vartheta \quad (\text{sferični koordinatni sistem})$$

$$\rho = \sqrt{x^2 + y^2} \quad \varphi = \arctan \frac{y}{x}$$

$$x = \rho \cos \varphi \quad y = \rho \sin \varphi$$

$$r = \sqrt{x^2 + y^2 + z^2} \quad \varphi = \arctan \frac{y}{x}$$

$$\vartheta = \arccos \frac{z}{\sqrt{x^2 + y^2 + z^2}}$$

$$x = r \sin \vartheta \cos \varphi \quad y = r \sin \vartheta \sin \varphi \quad z = r \cos \vartheta$$