

SINTAKSA JEZIKOV IN GRAMATIKE

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JEZIKI IN STAVKI

- Jezik = množica nizov (stavkov)
- Primeri stavkov in jezikov:

Zelo abstrakten jezik:

- ab, aabb, aaabbb, ...

Programski jezik:

- $x = a + b$
- if $x < y$ then $z = x$ else $z = y$

Naravni jezik:

- John paints.
- The cat scares a mouse.

DEFINICIJA JEZIKOV

- Definiramo sintakso in semantiko (pomen)
- Definicija sintakse navadno z *gramatiko*
- Definicija semantike, razni načini:
 - prevajalska semantika,
 - operacijska semantika
 - denotacijska
 - atributna gramatika
 - aksiomska
 - ...

DEFINIRANJE SINTAKSE Z GRAMATIKO (S PREPISNIMI PRAVILI)

Primer:

$$s \rightarrow a b$$
$$s \rightarrow a s b$$

s neterminalni simbol

a, b terminalna simbola

s začetni simbol

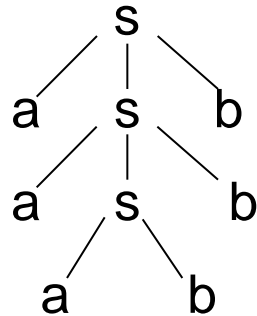
Krajši zapis:

$$s \rightarrow a b \mid a s b$$

GRAMATIKA GENERIRA STAVKE JEZIKA

$s \rightarrow a b$

$s \rightarrow a s b$



Generiranje od zgoraj navzdol

Generirani stavek (niz) = a a a b b b

Generirani stavek vsebuje samo terminalne simbole

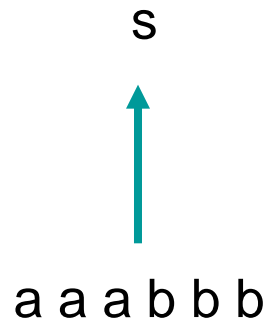
GRAMATIKA TUDI RAZPOZNAVA STAVKE JEZIKA

$s \rightarrow a b$

$s \rightarrow a s b$

Npr. dan je stavek $a a a b b b$

Ali stavek pripada jeziku?

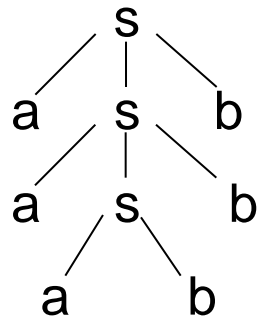


Razpoznavanje: od spodaj navzgor

SINTAKSNA RAZGRADNJA (SYNTACTIC PARSING)

Dani stavek: aaabbb

Sintaksna struktura stavka (sintaksno drevo, angl. parse tree):



BNF ZAPIS GRAMATIK BACKUS-NAUR FORM

$\langle s \rangle ::= a b \mid a \langle s \rangle b$

Koničasti oklepaji označujejo neterminalne simbole

IZRAZI V PROGRAMSKEM JEZIKU

$\langle \text{exp} \rangle ::= a \mid b \mid c \mid \dots$

$\langle \text{exp} \rangle ::= \langle \text{exp} \rangle + \langle \text{exp} \rangle \mid \langle \text{exp} \rangle * \langle \text{exp} \rangle$

$\langle \text{exp} \rangle ::= (\langle \text{exp} \rangle)$

Stavki tega jezika:

a

a + b

a + b * c

(a + b) * (a + c)

((a + b) * c)

...

Pazi: Ta gramatika lahko razgradi stavke na razne načine (*dvoumnost*)!

Gramatika je dvoumna (nezaželeno, dvoumen pomen)

ZAPOREDJA UKAZOV ZA ROBOTA

up

up up down up down

USTREZNA BNF GRAMATIKA

$\langle \text{move} \rangle ::= \langle \text{step} \rangle \mid \langle \text{step} \rangle \langle \text{move} \rangle$

$\langle \text{step} \rangle ::= \text{up} \mid \text{down}$

DCG GRAMATIKE

- DCG, Definite Clause Grammars
- *Definite Clause* = stavek v prologu (vendar ne vprašanje)
- Te gramatike so navadno vgrajene v prolog
- Prolog sam je že implementacija DCG gramatik
- Generira stavke in razgrajuje stavke

DCG ZA ROBOTOVE PROGRAME

move --> step.

move --> step, move.

step --> [up].

step --> [down].

PREDSTAVITEV STAVKOV V DCG

DCG pričakuje stavke kot „diferenčne sezname“ (difference list)

aabb ~ [a,a,b,b], []
~ [a,a,b,b,c], [c]
~ [a,a,b,b,x,y,z], [x,y,z]
~ ...

up up down up ~ [up, up, down, up], []
~ [up, up, down, up, left, right], [left, right]
~ [up, up, down, up | L], L

VPRAŠANJA ZA DCG

?- move([up,down,up], []).

yes

?- move([up, X, up], []).

X = up;

X = down;

no

?- move([up, down, up, a, b, c], [a, b, c]).

yes

PROLOG PREVEDE DCG V ANALIZNI PROGRAM

```
move( List, Rest) :-  
    step( List, Rest).
```

```
move( List1, Rest) :-  
    step( List1, List2),  
    move( List2, Rest).
```

```
step( [up | Rest], Rest).
```

```
step( [down | Rest], Rest).
```

PREVOD DCG V PROLOG

DCG rule:

move --> step, move.

Corresponding Prolog rule:

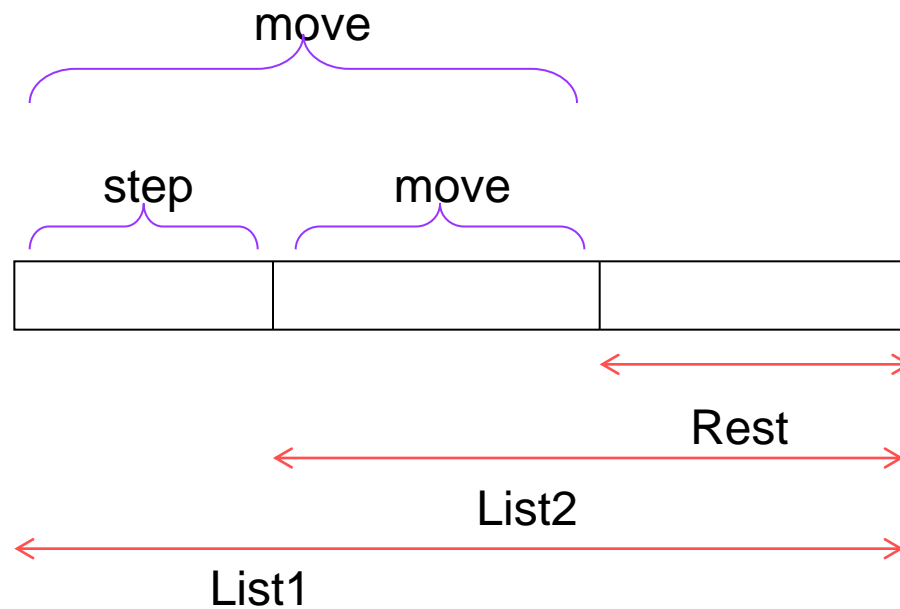
```
move( List1, Rest) :-  
    step( List1, List2),  
    move( List2, Rest).
```


DIFERENČNI SEZNAMI

- Omogočajo učinkovito konkatenacijo seznamov
- Deluje podobno kot kazalec na konec seznama
- Seznam L predstavljen s parom A - Z
A - Z predstavlja razliko med seznamoma A in Z
- Konkatenacija seznamov s konstantno časovno zahtevnostjo
 $\text{conc}(A1 - Z1, Z1 - Z2, A1 - Z2)$.

PREVOD DCG V PROLOG

```
move( List1, Rest) :-  
  step( List1, List2),  
  move( List2, Rest).
```



NALOGA

Prevedi v standardni Prolog:

$s \text{ --> } [a], s, [b].$

ENOSTAVNA DCG GRAMATIKA ZA ANGL. JEZIK

The *cat* *scares* *the* *mouse.*
| | | | |
det noun verb det noun



noun_phrase



noun_phrase



verb_phrase



sentence

ENOSTAVNA GRAMATIKA ZA ANGL.

sentence --> noun_phrase, verb_phrase.

verb_phrase --> verb, noun_phrase.

noun_phrase --> determiner, noun.

determiner --> [the].

noun --> [cat].

noun --> [cats].

noun --> [mouse].

verb --> [scares].

verb --> [scare].

TA GRAMATIKA GENERIRA STAVKE

[the, cat, scares, the, mouse]

[the, mouse, scares, the, mouse]

[the, cats, scare, the, mouse]

[the, cats, scares, the, mouse]

KONTEKSTNA ODVISNOST!



UJEMANJE V ŠTEVILU LAHKO VSILIMO Z ARGUMENTI

sentence(Number) -->
noun_phrase(Number), verb_phrase(Number).

verb_phrase(Number) -->
verb(Number), noun_phrase(Number1).

noun_phrase(Number) -->
determiner(Number), noun(Number).

noun(singular) --> [mouse].

noun(plural) --> [mice].

verb(singular) --> [scares].

verb(plural) --> [scare].

UJEMANJE V ŠTEVILU LAHKO VSILIMO Z ARGUMENTI

?- sentence(Number, [the, cats, scares, the, mouse], []).

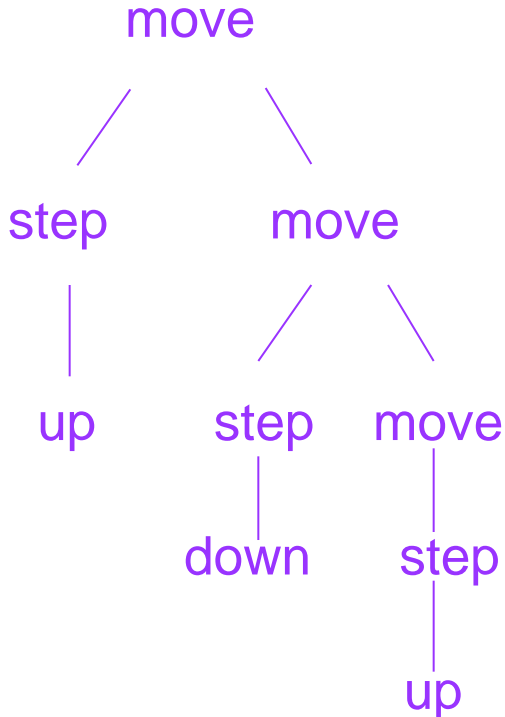
no

?- sentence(Number, [the, cats, scare, the, mouse], []).

Number = plural

KONSTRUIRANJE SINTAKSNIH DREVES

[up, down, up]



DCG, KI GRADI SINTAKSNA DREVESA

Tree = move(step(up), move(step(down), ...))

move(move(Step)) --> step(Step).

move(move(Step, Move)) -->
step(Step), move(Move).

step(step(up)) --> [up].

step(step(down)) --> [down].

DEFINIRANJE POMENA

N.pr.: Pomen od „move“ = Razdalja med začetno in končno točko

meaning ('up up down up') = $1+1-1+1 = 2$

meaning('up up down up') =
 meaning('up') + meaning('up down up')

OD SINTAKSNEGA DREVESA DO POMENA

Določitev pomena stavka:

- (1) Zgradi sintaksno drevo
- (2) Izlušči pomen iz sintaksnega drevesa

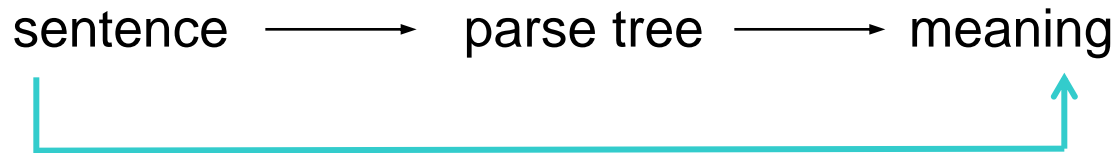
POMEN SINTAKSNIH DREVES ZA „MOVE“

meaning(move(Step, Move), Dist) :-
 meaning(Step, D1),
 meaning(Move, D2),
 Dist is D1 + D2.

meaning(move(Step), D) :-
 meaning(Step, D).

meaning(step(up), 1).
meaning(step(down), -1).

DRUGA MOŽNOST: PREPLETEMO SINTAKSO IN SEMANTIKO



Sintaksno drevo zaobidemo, pomen vgrajen direktno v gramatiko

PROLOGOVI CILJI V DCG: {Goal}

move(Dist) --> step(Dist).

move(Dist) -->
step(D1), move(D2), {Dist is D1 + D2}.

step(1) --> [up].

step(-1) --> [down].

?- move(D, [up, up, down, up], []).
D = 2

NALOGA

Naj bo dana naslednja gramatika:

$\text{move}(X_0, X) \rightarrow$
 $\text{step}(Dx), \{ X \text{ is } X_0 + Dx, \text{safe}(X) \}.$

$\text{move}(X_0, X) \rightarrow$
 $\text{step}(Dx), \{ X_1 \text{ is } X_0 + Dx, \text{safe}(X_1) \}, \text{move}(X_1, X).$

$\text{step}(1) \rightarrow [\text{right}].$

$\text{step}(-1) \rightarrow [\text{left}].$

$\text{safe}(X) :-$

$-5 \leq X, X \leq 5.$

NALOGA, NAD.

Kaj odgovori prolog na vprašanja:

(a) ?- move(2, Xa, [left,right,right,right], []).

(b) ?- move(4, Xb, [left,right,right,right], []).

(c) ?- conc(L, _ , _), move(5, 5 ,L, []). % conc is list concatenation
(Podaj prve tri prologove odgovore)

(d) Naj gramatika definira gibanje robota. Kaj pomenita X in Y v move(X,Y)? Intuitivno, kakšne premike robota dovoljuje ta gramatika?

NALOGA, NAD.

- (e) Ali lahko gramatiko uporabimo v obratni smeri: podamo „pomen“ stavka, kaj je stavek s tem pomenom? Npr. program za robota, ki premakne robota iz 4 v -3. Postavi ustrezno vprašanje.

NALOGA

Dana je naslednja gramatika:

$s(N, \text{Dir}) \rightarrow \text{num}(N)$.

$s(N1, \text{inc}) \rightarrow \text{num}(N1), s(N2, \text{inc}), \{N1 \leq N2\}$.

$s(N1, \text{dec}) \rightarrow \text{num}(N1), s(N2, \text{dec}), \{N1 \geq N2\}$.

$\text{num}(N) \rightarrow [N], \{N=1; N=2; N=3\}$.

Kaj prolog odgovori na naslednja vprašanja?

(a) ?- $s(N, \text{Da}, [2,3], [])$.

(b) ?- $s(N, \text{Db}, [2, 3, 4], [])$.

(c) ?- $s(N, \text{Dc}, [1, 3, 2], [])$.

(d) ?- $s(N, \text{Dd}, [2, 2, 2, 2])$. % Give all Prolog's answers

(e) ?- $s(2, \text{De}, [N1, N2], [])$. % Give all Prolog's answers

POMEN NARAVNEGA JEZIKA

- Kako predstaviti pomen stavkov naravnega jezika = ?
- Ena možnost je logika

PRIMERI POMENOV V LOGIKI

Stavek

Formalizirani pomen

``John paints``

paints(john)

``John likes Annie``

likes(john, annie)

PRIMERI POMENOV V LOGIKI

Stavek:

``A man paints''

Pomen:

exists(X, man(X) and paints(X))

Opomba: ``paints'' je netranzitivni glagol, ``likes'' je tranzitivni glagol

MOŽNA SINTAKSA

sentence ---> noun_phrase, verb_phrase.

noun_phrase --> proper_noun.

verb_phrase --> intrans_verb.

verb_phrase --> trans_verb, noun_phrase.

intrans_verb --> [paints].

trans_verb --> [likes].

proper_noun --> [john].

...

VGRADNJA POMENA

% "john" means "john"

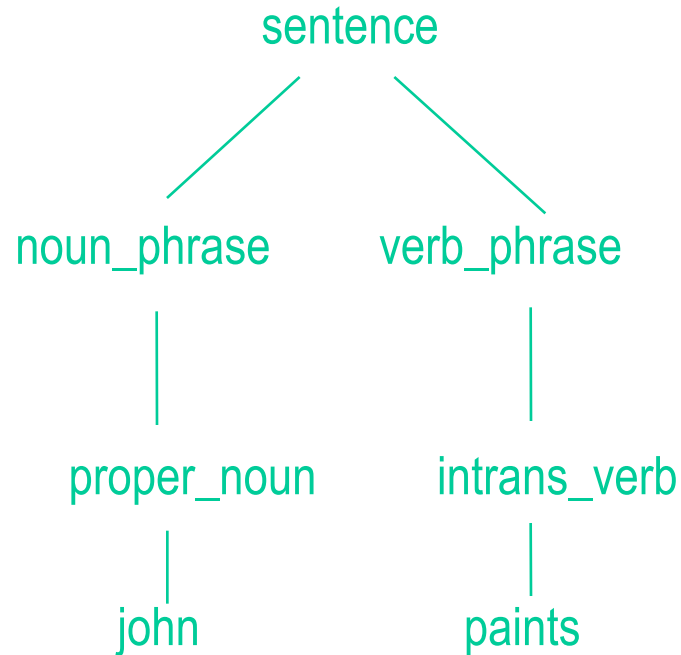
proper_noun(john) --> [john].

% "paints" means "paints(X)"

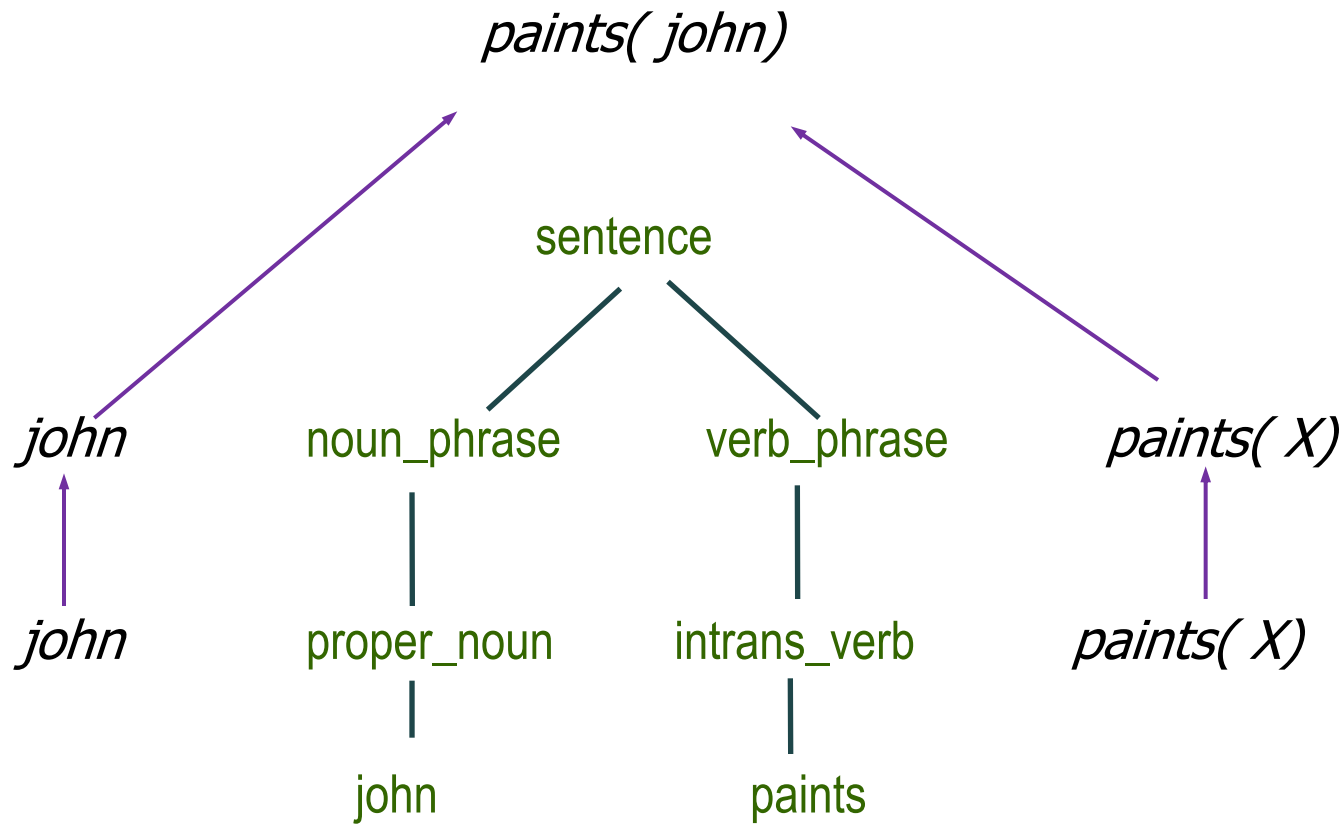
intrans_verb(paints(X)) --> [paints].

SESTAVLJANJE POMENOV SAMOSTALNIŠKE FRAZE IN GLAGOLSKE FRAZE

“John paints”



SESTAVLJANJE POMENOV SAMOSTALNIŠKE FRAZE IN GLAGOLSKE FRAZE



SESTAVLJANJE POMENOV FRAZ

john + *paints(X)* = *paints(john)*

Pomen NP

Pomen stavka

Pomen VP

SESTAVLJANJE POMENOV FRAZ

noun_phrase(NP) --> proper_noun(NP).

verb_phrase(VP) --> intrans_verb(VP).

sentence(S) --->

noun_phrase(NP), verb_phrase(VP),
{ compose(NP, VP, S) } .

SESTAVLJANJE POMENOV NP IN VP

compose(NP, VP, VP) :-

arg(1, VP, NP).

% 1st argument in VP is NP

?- compose(john, paints(X), S).

S = paints(john)


BOLJ ELEGANTNO

DEFINIRAJ POMEN GLAGOLA TAKO,
DA OSEBEK (AGENT) POSTANE DODATNI ARGUMENT


intrans_verb(Agent, paints(Agent)) --> [paints].

verb_phrase(Agent, VP) --> intrans_verb(Agent, VP).

sentence(VP) --->
noun_phrase(Agent), verb_phrase(Agent, VP).



S tem naredimo “predale“ vidne od zunaj

paints(Agent)



Predal, ki ga zapolnimo vsebino iz konteksta

POMEN TRANZITIVNIH GLAGOLOV

- “John likes Mary” pomeni *likes(john, mary)*
- “likes” pomeni *likes(Somebody, Something)*

trans_verb(Somebody, Something, likes(Somebody, Something)) -->
[likes].

verb_phrase(Somebody, VP) -->
trans_verb(Somebody, Something, VP),
noun_phrase(Something).

POMEN „DOLOČILNIKOV“ “A” IN “EVERY”

- “A man paints” pomeni:

exists(X, man(X) and paints(X))

- Določilnik “a” diktira pomen celega stavka!

- “a man” pomeni:

exists(X, man(X) and Assertion)



Trditev o X

KAJ POMENI “A”?

- “a” pomeni:

There is some X such that:

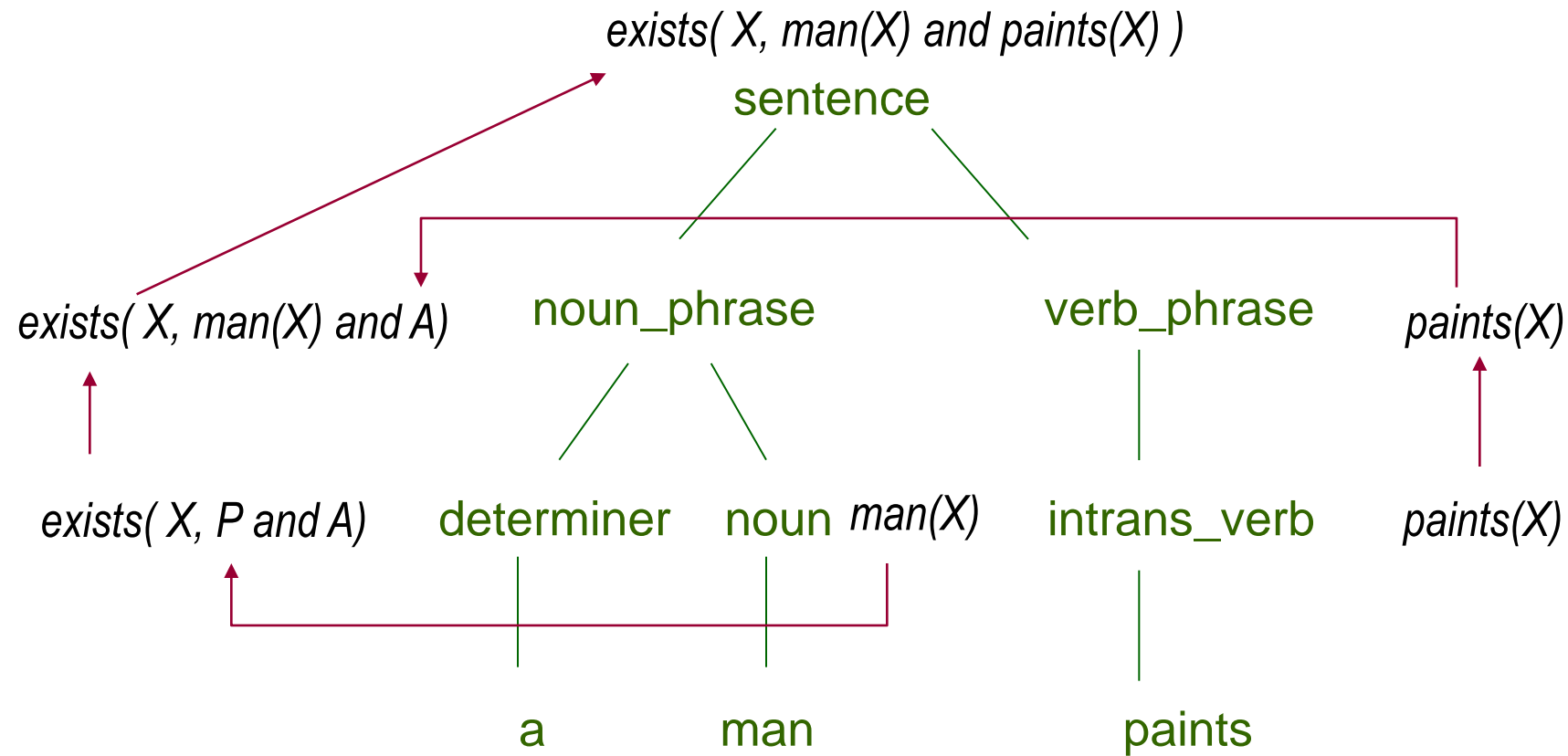
X has some property and
some assertion holds about X.

exists(X, Property and Assertion)

- Naredimo X, Property in Assertion vidne:

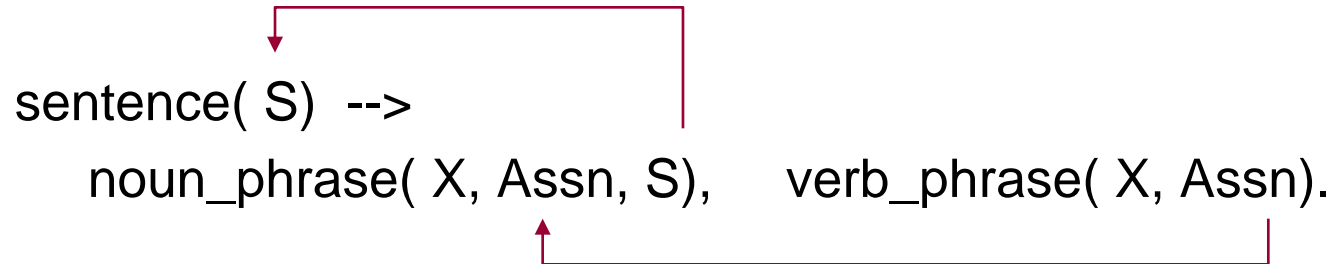
determiner(X, Property, Assn, exists(X, Property and Assn)) -->
[a].

INTEGRACIJA POMENOV DOLOČILNIKOV IN DRUGIH FRAZ

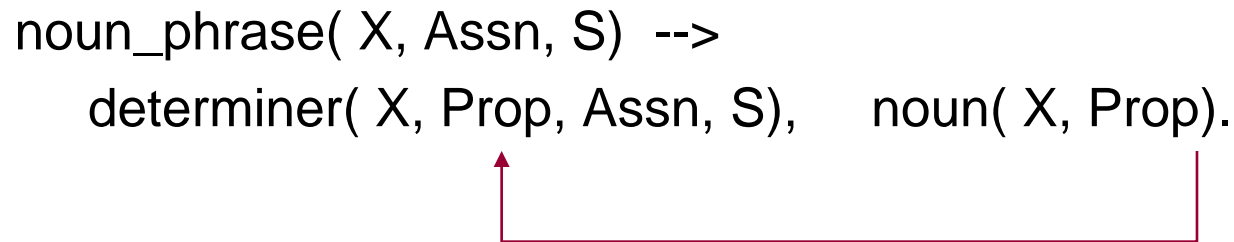


INTEGRACIJA POMENOV DOLOČILNIKOV IN DRUGIH FRAZ

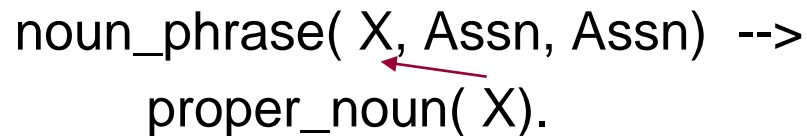
sentence(S) -->
noun_phrase(X, Assn, S), verb_phrase(X, Assn).



noun_phrase(X, Assn, S) -->
determiner(X, Prop, Assn, S), noun(X, Prop).



noun_phrase(X, Assn, Assn) -->
proper_noun(X).



INTEGRACIJA POMENOV DOLOČILNIKOV IN DRUGIH FRAZ

verb_phrase(X, Assn) -->
intrans_verb(X, Assn).

determiner(X, Prop, Assn, exists(X, Prop and Assn)) --> [a].

noun(X, man(X)) --> [man].

intrans_verb(X, paints(X)) --> [paints].

DOLOČILNIK “EVERY”

“Every woman dances” means:

$$\text{all}(X, \text{woman}(X) \implies \text{dances}(X))$$

determiner(X, Prop, Assn, all(X, Prop \implies Assn))
--> [every].

RELATIVNI STAVKI

“Every man that paints admires Monet”

SINTAKSA:

noun_phrase --> determiner, noun, rel_clause.

rel_clause --> [that], verb_phrase.

rel_clause --> []. % Empty relative clause

RELATIVNI STAVKI

“Every man that paints admires Monet”

POMEN:

all(X, man(X) and paints(X) ==> admires(X, monet))

NALOGA

Definiraj v logiki pomen naslednjih stavkov:

- (a) Every student of Newton did an experiment that involved gravity.
- (b) Every dog chases a cat that hates the dog.
- (c) Every dog chases a cat that hates a dog.

NALOGA, NAD.

(d) Every Italian cooks pasta.

(e) Every Italian in Peartree Village owns a restaurant that overlooks a bridge.

(f) A lady from the Information Office helps all customers that book a tour.

RELATIVNI STAVKI

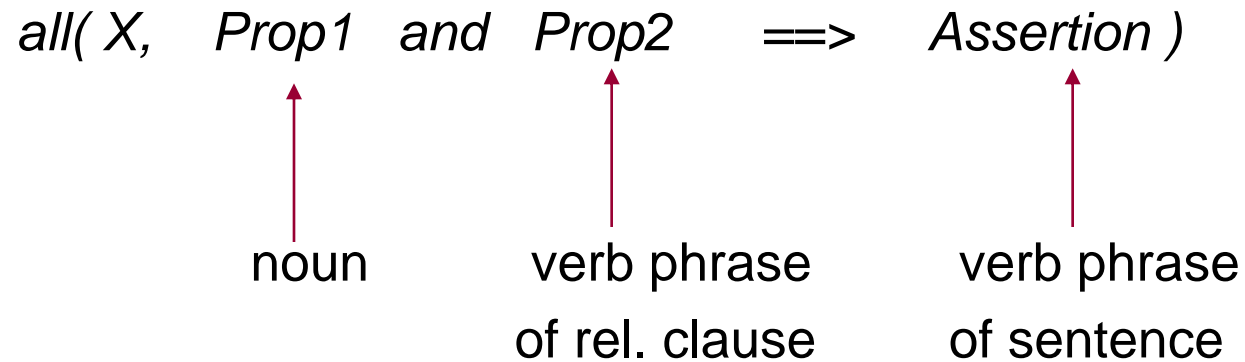
POMEN, SPLOŠNA OBLIKA

all(X, Prop1 and Prop2 ==> Assertion)

noun

verb phrase
of rel. clause

verb phrase
of sentence



RELATIVNI STAVKI: SINTAKSA IN POMEN

rel_clause(X, Prop1, Prop1 and Prop2) -->
[that], verb_phrase(Prop2).

noun_phrase(X, Assn, S) -->
determiner(X, Prop12, Assn, S), noun(X, Prop1),
rel_clause(X, Prop1, Prop12).

rel_clause(X, Prop1, Prop1) --> [].

KOMPLETNA GRAMATIKA

% Meaning of subset of natural language

:- op(100, xfy, and).

:- op(150, xfy, =>).

sentence(S) -->

noun_phrase(X, P, S), verb_phrase(X, P).

noun_phrase(X, P, S) -->

determiner(X, P12, P, S), noun(X, P1), rel_clause(X, P1, P12).

noun_phrase(X, P, P) -->

proper_noun(X).

verb_phrase(X, P) -->

trans_verb(X, Y, P1), noun_phrase(Y, P1, P).

verb_phrase(X, P) -->

intrans_verb(X, P).

KOMPLETNA GRAMATIKA, NAD.

rel_clause(X, P1, P1 and P2) -->
[that], verb_phrase(X, P2).

rel_clause(X, P1, P1) --> [].

determiner(X, P1, P, all(X, P1 => P)) --> [every].

determiner(X, P1, P, exists(X, P1 and P)) --> [a].

noun(X, man(X)) --> [man].

noun(X, woman(X)) --> [woman].

proper_noun(john) --> [john].

proper_noun(annie) --> [annie].

proper_noun(monet) --> [monet].

trans_verb(X, Y, likes(X, Y)) --> [likes].

trans_verb(X, Y, admires(X, Y)) --> [admires].

intrans_verb(X, paints(X)) --> [paints].

PRIMERI STAVKOV, KI JIH RAZUME TA GRAMATIKA

“Every man that paints admires Monet”

“Annie admires every man that paints”

“Every woman that admires a man that paints likes Monet”

Gramatika za ta stavek zgradi naslednji pomen:

*all(X, woman(X) and exists(Y, (man(Y) and paints (Y))
and admires(X, Y)) ==> likes(X, monet))*

TESTNI STAVKI

% Some tests

test1(M) :-

 sentence(M, [john,paints],[]).

test2(M) :-

 sentence(M, [a, man, paints], []).

test3(M) :-

 sentence(M, [every,man,that,paints,admires,monet],[]).

test4(M) :-

 sentence(M, [annie,admires,every,man,that,paints],[]).

test5(M) :-

 sentence(M, [every,woman,that,admires,a,man,that,paints,likes,monet],[]).

NALOGA

Naslednje pravilo skuša definirati pomen določilnika „every“:

determiner(X, Prop, Assn, all(X, Prop and Assn)) --> [every].

- (a) Ali je pravilo pravilno? Če ni, predlagaj popravek.
- (b) Kakšno vlogo imata argumenta Prop in Assn? Katere stavčne fraze določajo vrednost Prop in Assn?

UPORABA V ODGOVARJANJU NA VPRAŠANJA

Pomeni v logiki se lahko izrazijo tudi v prologu:

admires(X, monet) :-
man(X), paints(X).

admires(annie, X) :-
man(X), paints(X).

likes(X, monet) :-
woman(X), man(Y), paints(Y), admires(X, Y).

“Does Annie admire anybody who admires Monet?”

?- admires(annie, X), admires(X, monet).

GENERIRANJE STAVKOV

- Naša gramatika lahko tudi generira stavke v z dani pomenom:

?- sentence(likes(john,annie), S, []).

S = [john, likes, annie]

?- sentence(exists(X, man(X) and paints(X)), S, []).

S = [a, man, paints]

PREVAJANJE MED JEZIKI Z DCG

- Prevod iz jezika 1 v jezik 2:

```
?- ...,  
    sentence_lang1( Meaning, Sent1, []),  
    sentence_lang2( Meaning, Sent2, []).
```

- Lahko uporabimo tudi za prevajanje programskih jezikov

```
?- ...,  
    program_source( M, SourceProg, []),    % Parse  
    program_target( M, TargetProg, []).    % Generate
```

KOMPLEKSNOST NARAVNEGA JEZIKA

An example that illustrates how hard it is to handle NL perfectly. The meaning also depends on the stress – which word in a sentence is stressed. Here is an example in which EACH word can be stressed, and each variant has different meaning:

I never said she stole my money.

Possibilities are:

I never said she stole my money.

I **never** said she stole my money.

I never **said** she stole my money.

I never said **she** stole my money.

I never said she **stole** my money.

I never said she stole **my** money.

I never said she stole my **money**.