

## 1. The system of equations

$$x - y + z - w = 1$$

$$x + y - z - w = 3$$

determines a two-dimensional plane in  $\mathbb{R}^4$ . Let  $T(0, -1, -1, 2)$ . Our objective is to find the point on the plane which is closest to  $T$ .

- (a) Write the matrix  $A$  and the right-hand side  $\mathbf{b}$  of the system above.
- (b) Evaluate  $A^+$ . (This is simple since  $A$  has full rank).
- (c) Show that  $P = I - A^+A$  is an orthogonal projection, meaning that  $P^2 = P$  and  $P^T = P$ . Onto which subspace does it project?
- (d) Express and compute the solution using  $A^+$ .
- (e) Write the function  $pT = \text{projekcija}(A, \mathbf{b}, T)$ , which returns the projection of the point  $T$  on to the hyperplane defined by the system  $A\mathbf{x} = \mathbf{b}$ .